Constraint-Based Workshops

 Transcriptional Regulatory Constraints February 28th, 2008



APPL. ENVIRON. MICROBIOL.



FIG. 7. Analysis of aerobic batch culture showing time profiles of cell density, glucose concentration, and acetate (Ac) concentration. The culture was not limited for minerals. The solid lines are the flux balance model predictions of the time profiles for the culture. E, average deviation between predictions of the model and experimental measurements.

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In Batch Culture: V is Constant Biomass (X) increases over time Carbon Source (eg. glucose) decreases over time

*Acetate is secreted if not enough Oxygen is supplied



Varma and Palsson, App. Environ. Microbiol. 60(10): 3723-3731 (1994)

How Can You Regulate Protein Levels?

- Adjust the rate of mRNA synthesis.
 TRANSCRIPTIONAL REGULATION
- Adjust the rate of mRNA translation.
 TRANSLATIONAL REGULATION
- Adjust the activity of proteins through post-translational modifications.
 - FOLDING, CLEAVAGE, SPLICING (INTEINS), CHEMICAL MODIFICATION

Transcriptional Regulation in Prokaryotes

- RNA polymerase
- Modes of regulation
 - Regulated recruitment
 - Activation of RNA polymerase
 - Promoter activation
 - Antitermination and attenuation

E. coli RNA Polymerase



holoenzymes

Ptashne, Genes & Signals, Figure 1.1

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NOTE: Another subunit w is associated with RNA polymerase, if deleted growth is reduced.

Mode 1: Regulated Recruitment

- Transcription factors (TFs) bind to specific binding sites in the promoter region of a gene
- After binding to DNA TFs either enhance (activator) or disrupt (repressor) RNA polymerase binding to DNA



Three States of the *lac* Genes



Ptashne, Genes & Signals, Figure 1.3



Mode 2: Activation of RNA Polymerase

NtrC acts on pre-bound polymerase.

Subsequent ATP hydrolysis induces conformational change.

NtrC activation is not dependent on DNA binding domain





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Ptashne, Genes & Signals, Figure 1.19

Mode 3: Promoter Activation

Normally, the -10 and -35 regions are separated by 17 nucleotides.

The merT promoter is separated by 19 nucleotides.



Ptashne, Genes & Signals, Figure 1.20

Mode 4: Regulate Termination by Attenuation

Transcription and translation are coupled in prokaryotes \bullet and the rate of translation can affect termination.

Tryptophan Leader Sequence (20 AA): MKAIFVLKGWWRTS



Mode 5: Regulate Termination by Antitermination

- RNA polymerase can stall during translation of genes
- Protein binding at various sites can allow the RNA polymerase to continue translation and prevent termination.
- Proteins "modify" the RNA polymerase and allow for it to resist terminators.
- Examples include: phage λ (nusABEG, N and Q proteins)

How Can We Incorporate Regulatory Constraints into Constraint-Based Models?

- We need to be able model how 100s of genes are regulated.
- We need to be able to account for how gene expression affects fluxes in constraint-based models.

Boolean Formalism

- Assume that genes are in one of two states:
 - Gene is Expressed
 - Gene is Not Expressed
- If genes needed for a reaction are not expressed then the reaction can not occur.
- With FBA and other methods, we assume that all enzymes & reactions are available for a cell to use.
- NOTE: Regulation of essential genes is not amenable to a Boolean approach

Regulation: Shaping the Space



No 'green': solution achievable but solution space smaller



No 'red': solution not achievable

- 1. Temporary, adjustable constraints
- 2. Flux(es) constrained to zero
- 3. Extreme vector(s) removed
- 4. Dimension or volume of space is reduced

Covert, Schilling and Palsson, JTB 2001

Regulatory Network File

- Medium Components (uptake & secretion rates)
- Transcription Factor Activity Status
- Metabolic Gene Expression Status
- Reaction Status (if all genes needed are expressed reaction is allowed)

sets genes /aceA, aceB, ackA, acnA, acnB, adhE, adk, aceE, aceF atpA, atpB, atpC, atpD, atpE, atpF, atpG, atpH, atpI crr, cydA, cydB, dctA, dcuC, eno, fba, fbp, focA, frdA, frdB, frdC, frdD fumA, fumB, fumC, gapA, gltA, gnd, icdA, ldhA, lpdA, maeB, mdh nuoA, nuoB, nuoE, nuoF, nuoG, nuoH, nuoI, nuoJ, nuoK, nuoL, nuoM, nuoN pckA, pfkA, pfkB, pflA, pflB, pflC, pflD, pgi, pgk, pgl, pgm, pitA, pitB pntA, pntB, ppc, ppsA, pta, ptsG, ptsH, ptsI, pykA, pykF, rpe, rpi sdhA, sdhB, sdhC, sdhD, sfcA, sucA, sucB, sucC, sucD, talA, tktA, tktB, tpi, zwf/

transcriptionfactors /Fnr,ArcA,DcuS,DcuR,FadR,IclR,Mlc,PdhR,Cra/

components(i) /ac_e,akg_e,etoh_e,formate_e,fumarate_e,glcD_e,lacD_e,o2_e,pyr_e,succ_e/;

parameters reactionstatus(j)
 genestatus(genes)
 TFstatus(transcriptionfactors)
 medium(components)
 temp1
 temp2;

genestatus(genes)=1; reactionstatus(j)=1;

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v from FBA V OUTPUT: ReactionStatus (0 or 1)

INPUT:

```
ne What is Present in the Medium (Substra
if((LowerLimits('EX ac e')<0) or (v.1('EX ac e')>0), medium('ac e')=1;
        else medium('ac e')=0;);
if((LowerLimits('EX akg e')<0) or (v.1('EX akg e')>0). medium('akg e')=1:
        else medium('akg e')=0;);
                                          If the lower limit is negative
if((LowerLimits('EX etoh e')<0) or (v.1('EX
        else medium('etoh e')=0;);
                                         OR if the FBA solution predicts
if((LowerLimits('EX for e')<0) or (v.l('EX i</pre>
        else medium('formate e')=0;);
                                         secretion, then the metabolite
if((LowerLimits('EX fum e')<0) or (v.1('EX )
                                              would be present in the
        else medium('fumarate e')=0;);
if((LowerLimits('EX glc e')<0) or (v.1('EX (
                                                         medium.
        else medium('glcD e')=0;);
if((LowerLimits('EX lacD e')<0) or (v.1('EX</pre>
        else medium('lacD e')=0;);
if((LowerLimits('EX o2 e')<0) or (v.1('EX o2
                                         Medium values are 0 if absent
        else medium('o2 e')=0;);
if((LowerLimits('EX pyr e')<0) or (v.1('EX p
                                                      & 1 if present
        else medium('pyr e')=0;);
if((LowerLimits('EX_succ_e')<0) or (v.1('EX_succ_e')>0), mealum('succ_e')=1;
        else medium('succ e')=0;);
                              *******
     etermine Transcription Factor Activities (0=Active, 1=Inactive
TFstatus('Fnr')=1-medium('o2 e');
                                           TF Status are Determined by
TFstatus('ArcA')=1-medium('o2 e');
TFstatus('DcuS')=medium('succ e');
                                          Medium Components & Some
TFstatus('DcuR')=TFstatus('DcuS');
TFstatus('FadR')=max(medium('glcD e'),1-mediv
                                                  Intracellular Fluxes
TFstatus('IclR')=TFstatus('FadR');
TFstatus('Mlc')=1-medium('glcD e');
```

Translating Boolean Rules in GAMS:

**Here X,Y,Z are binary (0/1), and represent genes, TFs, media components

- Z active if X
- Z active if NOT X Z = 1-X
- Z active if X AND Y Z = min(X,Y)
- Z active if X OR Y Z = max(X,Y)
- Eq. Fnr is active when $Fnr=1-medium(O_2)$ O₂ is NOT in the medium
- Eg. FadR is active Glucose is present OR acetate is absent from medium.

- Z = X

- FadR=max[medium(glc) ,1-medium(ac)]



Gene to Reaction Associations

- If necessary genes are expressed (ie. genestatus =1) then the reaction status is 1, meaning the reaction can happen.
- Otherwise, if the necessary genes aren't all expressed then the reaction status is 0, meaning reaction can not occur.





Output Text File

"Model status:	н	1.00								
"Solver status:		1.00								
"Rxn Abbr"	"FBA So	lution"	"Reactio	on Status	(0=0ff,	1=On)"		"rFBA Sol	ution"	
"EX_ac_e"	0.0000	1	1.5639							
"EX_akg_e"	0.0000	1	0.0000							
"EX_co2_e"	9.1599	1	7.7815							
"EX_etoh_e"	0.0000	1	0.0000				"Iransc	ription r	actor Sta	tus (0=inctive, 1=Active)"
"EX_for_e"	0.0000	1	0.0000				"Fnr"	0		
"EX_fum_e"	0.0000	1	0.0000				"Arca"	0		
"EX_glc_e"	-5.0000		1	-5.0000			"Deus"	0		
"EX_h_e"	5.1807	1	6.3098				"Deuk"	0	-	
"EX_h2o_e"	10.0569		1	8.6032			"Fack"			adk, ICIK, and
"EX_lacD_e"	0.0000	1	0.0000				"ICIR"			, , , , , , , , , , , , , , , , , , ,
"EX_02_e"	-8.5938		1	-7.2629			"MIC"	0	PdhR	are Active
"EX_pi_e"	-1.8015		1	-1.6503			"Pank"	1		
"EX_pyr_e"	0.0000	1	0.0000				CIA	0		
"EX_succ_e"	0.0000	1	0.0000				Cono F	www.aation	Status (0-0ff 1-0-0 "
"ACKr" 0.0000	1	-1.5639)				"Gene r	1 Apression	Status (0-011, 1-01).
"ACONT"	1.9175	1	0.4840				"ENO"	1		
"ACt2r"	0.0000	1	-1.5639				UED2 U	1		
"ADHEr"	0.0000	1	0.0000				"FBD"	1		
"ADK1" 0.0000	1	0.0000					"CND"	1		
"AKGt2r"	0.0000	1	0,0000.					1		
"ATPM" 0.000	ι(FBA)).000(μ(rFBA)				"PGT"	1		
"ATPS4r"		_	ī	3393			"PGK"	1 11		a a / a b d a a a D
"Biomass"	0.4897	1	0.4486				"PGT."	; H(ere a	
"CO2t" -9.1599	Do	action	-7.7815				"PGM"	1		-
"CS" 1.9175	1 10	action					"PPC"	ar ar	e noi	Expresses
"CYTBD"	^{17.1} St	tatus	14.5257				"BPF"	1		
"DLACt2"	0.0	-	0.0000				"RPT"	1		
							"TALA"	1		
							"TPI"			
			0 D' I				"aceA"	0		
UW-Madis	on, Che	emical	& BIOIO	gical Eng	gineeri	ing	"aceB"	0		

Regulatory Model Calculations Part 1

- What are the growth rate predictions for glucose aerobic growth using FBA & rFBA (glucose uptake = 5)?
- What reactions are not available during glucose aerobic growth? What about during glucose anaerobic growth?
- What are the growth rate predictions if you remove PPC (phosphoenolpyruvate carboxylase: pep to oaa) for glucose aerobic growth?

Regulatory Model Calculations Part 1 Ans

• What are the growth rate predictions for glucose aerobic growth using FBA & rFBA?

- ANS: FBA = 0.49 and rFBA = 0.45

- What reactions are not available during glucose aerobic growth? What about during glucose anaerobic growth?
 - Aerobic: FORt, FRD, ICL, MALS, PFL, PPS, AKGDH, SUCCt2b,
 - Anaerobic: ICL, MALS, MDH, PDH, PPS, AKGDH, SUCD1i, SUCD4,
- What are the growth rate predictions if you remove PPC (phosphoenolpyruvate carboxylase) for glucose aerobic growth?

- ANS: FBA = 0.49 and rFBA = 0

Regulatory Model Calculations Part 2

- What are the growth rate predictions if you remove PDH (pyruvate dehydrogenase: pyr to accoa) for glucose aerobic growth?
- What enzymes would you need to express if you wanted the cells to grow aerobically on glucose without PDH? (hint: look at the reduced costs for removed reactions)
- Is it possible for rFBA to find a non-zero growth rate if FBA finds a zero maximum growth rate?

Regulatory Model Calculations Part 2 Ans

• What are the growth rate predictions if you remove PDH for glucose aerobic growth?

- ANS: FBA = 0.46 and rFBA = 0

 What enzymes would you need to express if you wanted the cells to grow cells to grow aerobically on glucose without PDH? (hint: look at the reduced costs for removed reactions)

– ANS: PFL (and PDH but this was deleted)

- Is it possible for rFBA to find a non-zero growth rate if FBA finds a zero maximum growth rate?
 - ANS: No, rFBA should always find a smaller flux through your objective function than FBA. Regulated solution space is a subspace of unregulation solution space.

Glucose Aerobic Growth



- rFBA correctly predicts the time delay before acetate is reconsumed.
- rFBA can be used to predict gene expression measurements.

MW Covert & BO Palsson. J Biol Chem. 277(31): 28058-64 (2002).



Diauxic Growth: Glucose vs. Lactose



- FBA incorrectly predicts that glucose and lactate will be consumed simultaneously.
- rFBA can be used to predict gene expression measurements.

MW Covert & BO Palsson. J Biol Chem. 277(31): 28058-64 (2002).



rFBA Can Correct FBA Over Predictions

- rFBA correctly predicts that some gene deletions are lethal.
 - Pyruvate dehydrogenase for glucose or succinate aerobic growth.
 - Phosphoenolpyruvate carboxylase for glucose or glycerol aerobic growth
 - Can predict TF knockout effects
- Overall, rFBA correctly predicted 106/116 cases (different mutants under different conditions)

MW Covert & BO Palsson. J Biol Chem. 277(31): 28058-64 (2002). UW-Madison, Chemical & Biological Engineering TABLE I Comparison of experimental mutant studies with in silico predictions of the FBA and rFBA models under various conditions

Results are scored as + or - meaning growth or no growth determined from *in vivo*/FBA/rFBA data. An N blank indicates that data were not available for these conditions. Cases where rFBA makes a correct prediction either unpredicted or incorrectly predicted by FBA alone are denoted by a shaded box. In 106 of 116 cases, the rFBA prediction matches the experimentally observed behavior. gl, glycerol; suc, succinate; $(-O_2)$, anaerobic conditions.

	glc	gl	suc	ac	rib	glc (-O ₂)	Dual Substrates	Ref
aceA	+/+/+		+/+/+	-/-/-		+/+/+		21
aceB				-/-/-				22
aceEF	-/+/-		-/+/-	+/+/+		+/+/+	(glc-ac) +/+/+	23
ackA	Territoria (Statute of the	+/+/+				24
ackA + pta + acs				-1-1-				24
acnă	+/+/+	+/+/+	+/+/+	+/+/+		+/+/+		22,25
acnB*	+/+/+	+/+/+	+/+/+	-/+/+		+/+/+		25
pgk	-/-/-	-/-/-	-1-1-				(gl-suc) +/+/+	28
pgl	+/+/+							29
ppg	-1.1-	-1+1-	+/+/+				(gl-suc) +/+/+	29.31

(glc-suc)

+/+/+

High-Throughput Phenotyping Data Knockout Strains



HT Phenotyping/Model Comparison							
exp/met/reg		Percent					
Reg and Met models predict correctly							
+/+/+	6222	45.3%					
-/-/-	2094	15.2%					
Reg model predicts correctly							
-/+/-	657	4.8%					
+/-/+	0	0.0%					
+/n/+	1350	9.8%					
-/n/-	505	3.7%					
Met model only predicts correctly							
+/n/-	242	1.8%					
-/n/+	153	1.1%					
-/-/+	0	0.0%					
+/+/-	257	1.9%					
Neither model predicts correctly							
-/+/+	702	5.1%					
+/-/-	1568	11.4%					
Met	8968	65.2%					
Reg	10828	78.7%					
Total	13750	100.0%					

Total Consistency: 10,828 (78.7%)

ASAP Database (Glasner et al., 2003)

- 125 Environments, 110 Strains
 - 13,750 Cases Overall

UW-Madison, Chemical & BiCovert, et al. Nature, 429: 92-96 (2004).



Network Elucidation



Reconciling the model with measured phenotypes leads to specific hypotheses

- Thymidine as a carbon source: not predicted by model
 - Thymine transporter is missing
- Arginine biosynthesis: essential to model, knockout strain grows
 - Reversibility of certain enzymes (YgjG, SpeC or SpeR, AldH or Prr) enables the *in silico* strain to produce arginine
 - *ilvY* strain: lethal in model due to essentiality of IlvC (15-fold shift)
 - Intervention of another factor
 - Sufficient basal level of IIvC activity
 - Uncharacterized IIvC isozyme

Covert, et al. Nature, **429**: 92-96 (2004).

Gene Expression Data

Aerobic/Anaerobic Shift

- Affymetrix gene chips/qPCR for +/- O2
- 437 Significant Shifts (P <0.007, FDR = 5%)</p>
- 151 altered genes included in the model
- Original model
 - Model predictions of all conditions for comparison
 - 75 predicted shifts (28:NA)
 - Model predicts 23 shifts correctly
 - 23/151 = 15% coverage
 - 23/(75-28) = 49% accuracy

Shift Comparisons

(predicted: experimental)					
Pred Total 75					
Exp Total 437					
Ex	p in Model	151			
1	(P:E)	23			
2	(0:0)	606			
3	(P:-E)	1			
4	(P:0)	23			
5	(0:E)	127			
No comparison possible					
	(P:NA)	28			
	(0:NA)	197			
	(NM:E)	286			
	(NM:0)	2067			
(NM:NA)	989			

Regulatory Network Interrogation



Model-Centric Hypothesis Generation

• Systematic network perturbation

- Locate significant shifts in WT
- $\Delta arcA^{-}, \Delta fnr^{-}, \Delta arcA^{-}fnr^{-}, \Delta appY^{-}, \Delta oxyR^{-}, \Delta soxS^{-}$
- ANOVA to identify rules
- Observations
 - Most rules unaffected by all KO strains
 - Still TFs/effects to identify
 - Complex rules ($\Delta arcA^{-}$ or Δfnr^{-} but not $\Delta arcA^{-}fnr^{-}$)
 - Microaerobic as in *cydAB*
 - Indirect metabolic/regulatory effects (Cra)
 - TF expression and activity correlation
 - arcA: positive correlation
 - fnr, bet1, fur: negative correlation



Recommended Reading

- Covert MW, Knight EM, Reed JL, Herrgard MJ, Palsson BO. Integrating high-throughput and computational data elucidates bacterial networks. Nature. 2004 May 6;429(6987):92-6.
- Covert MW, Palsson BØ. Transcriptional regulation in constraints-based metabolic models of Escherichia coli. J Biol Chem. 2002 Aug 2;277(31):28058-64.
- Covert MW, Schilling CH, Palsson B. Regulation of gene expression in flux balance models of metabolism. J Theor Biol. 2001 Nov 7;213(1):73-88.